## What is Physics?

Physics studies $\qquad$ that can be $\qquad$ with our five senses.

Model - $\qquad$
Theory - $\qquad$
Law - Uses $\qquad$ language to describe $\qquad$ patterns that have been verified $\qquad$ times

Scientific Method - used to solve many types of problems, not just science
Usually begins with $\qquad$ and question about the phenomenon to be studied
Next preliminary research is done and $\qquad$ is developed
Then experiments are performed to $\qquad$ the hypothesis
Finally the tests are analyzed and a $\qquad$ is drawn

## Units

Science uses $\qquad$ System (SI System)

Base Units
Length - $\qquad$ (m)

Time - $\qquad$ (s)

Mass - $\qquad$ (kg)

Others are $\qquad$ units

## Unit Conversions

| Prefix | Symbol | Value | Prefix | Symbol | Value |
| :---: | :---: | :---: | :---: | :---: | :---: |
| exa | $E$ | $10^{18}$ | deci | d | 10-1 |
| peta | $\boldsymbol{P}$ | $10^{15}$ | centi | c | 10-2 |
| tera | T | $10^{12}$ | milli | m | 10-3 |
| giga | G | $10^{9}$ | micro | $\boldsymbol{\mu}$ | 10-6 |
| mega | M | $10^{6}$ | nano | $n$ | 10-9 |
| kilo | $k$ | $10^{3}$ | pico | $p$ | 10-12 |
| hecto | $h$ | $10^{2}$ | femto | $f$ | 10-15 |
| decka | $d a$ | $10^{1}$ | atto | $a$ | 10-18 |

Multiply by $\qquad$ factors so that unwanted units out
Convert 20 Gm to m

## Convert 5 cg to kg

Convert $25 \mathrm{~km} / \mathrm{h}$ to $\mathrm{m} / \mathrm{s}$

## Accuracy and Precision

Accuracy is how $\qquad$ a measurement is to the value for that measurement.
Precision of a measurement system is refers to how $\qquad$ the agreement is between $\qquad$ measurements.

Accuracy and precision mean there is some $\qquad$ .
A device can repeatedly get the same $\qquad$ (precise), but always be $\qquad$ (not accurate).


Used to reflect ______ in measurements
Each measuring device can only measure so accurately
The $\qquad$ digit is always an $\qquad$

To find significant figures Ignore $\qquad$ zeros between the decimal point and the first nonzero digit
Count the number of other $\qquad$
0.000000602

1032000
1.023

## Rules for combining significant figures

## Addition or subtraction

The answer can contain no more $\qquad$ places than the $\qquad$ precise measurement.
$1.02+2.0223=$

## Multiplication or division

The result should have the same number of $\qquad$ as the quantity having the $\qquad$ significant figures entering into the calculation.

```
1.002 \cdot2.0223=
```


## Homework

1. Classify each as a model, theory, or law.
a. $\qquad$ Bohr model of atom
b. $\qquad$ Gravity
c.

## problem

d. $\qquad$ The Earth is round
e. $\qquad$
f. ___Creation
2. The altitude of the International Space Station is 409 km . What is this in meters? (RW) $\mathbf{4 0 9 0 0 0} \mathbf{~ m}$
3. The elevation of Berrien Springs is 209 m . What is this in cm? (RW) 20900 cm
4. Convert 1 hour to seconds. (RW) $\mathbf{3 6 0 0} \mathbf{~ s}$
5. The speed limit on some highways is $100 \mathrm{~km} / \mathrm{h}$. How fast is that in $\mathrm{m} / \mathrm{s}$ ? (RW) $27.8 \mathrm{~m} / \mathrm{s}$
6. The Earth orbits the sun at $29.78 \mathrm{~km} / \mathrm{s}$. What is this in km/h? (RW) 107200 km/h
7. The Earth orbits the sun at $29.78 \mathrm{~km} / \mathrm{s}$. What is this in mph (assume 1 mile $=1.609 \mathrm{~km})$ ? $(\mathrm{RW}) 66630 \mathrm{mph}$
8. The surface area of the Earth is $510,072,000 \mathrm{~km}^{2}$. What is

9. Water covers approximately $361,132,000 \mathrm{~km}^{2}$ of the Earth's surface. What is this in $\mathrm{ft}^{2}$ (assume $1 \mathrm{~m}=3.2808 \mathrm{ft}$ )? (RW) $\mathbf{3 . 8 8 7 1} \times \mathbf{1 0}^{\mathbf{1 5}} \boldsymbol{f t}^{\mathbf{2}}$
10. The average density of Earth is $5.514 \mathrm{~g} / \mathrm{cm}^{3}$. What is this in $\mathrm{kg} / \mathrm{m}^{3}$ ? (RW) $5514 \mathrm{~kg} / \mathrm{m}^{3}$
11. $148,940,000 \mathrm{~km}^{2}$ of land are on Earth. How many significant figures are in this number? (RW) 5
12. During the breeding season, an adult Monarch Butterfly will live 0.0760 yrs. How many significant figures? (RW) 3
13. The village of Berrien Springs covers $2.64 \mathrm{~km}^{2}$. How many significant figures? (RW) 3
14. $0.21 \mathrm{~km}^{2}$ of Berrien Springs is water. How many significant figures? (RW) 2
15. Using the information from the previous two questions, how much land is there in Berrien Springs? How many significant figures should be in your answer? (RW) 2.43 $\mathbf{k m}^{2}, 3$
16. If there are about 740 people per $\mathrm{km}^{2}$ in Berrien Springs (living on the land), how many people live in Berrien Springs? How many significant figures should be in your answer? (RW) $\mathbf{1 8 0 0}$ people, 2

## Kinematics

Studies $\qquad$ without thinking about its $\qquad$

## Position (x)

The $\qquad$ where something is relative to a $\qquad$ system called a $\qquad$
The most common coordinate system the $\qquad$ coordinate system

## Displacement ( $4 x$ )

The change in position
$\qquad$ and
Path does $\qquad$ matter
Only $\qquad$ and $\qquad$ position matters

What is the displacement of the path in the diagram?


## Distance

The $\qquad$ of the path traveled

Has only $\qquad$

You drive 20 km east, then turn around and drive 15 km west. What is your displacement?

What was your distance traveled?

1. What was difficult about measuring the $3 x 5$ card? Why?
2. How are distance and displacement the same? How are they different?
3. How are scalars and vectors the same? How are they different?
4. Classify each measurement as a scalar or vector.
a. ___ 20 books on a shelf
b. $\qquad$ A car travels 25 km east
c. $\qquad$ A plane flies 500 km
d. $\qquad$ The car drives $100 \mathrm{~km} / \mathrm{h}$ west
e. ___ The plane flies 200 mph north
$\qquad$
5. The road I live on goes east and west. One day, my family and I decide to go west to the beach. I travel 2 miles west when my wife realizes we passed a flock of wild turkeys. I turn around and drive back $1 / 2$ miles before we find the turkeys. What is my displacement at the flock of turkeys (make west negative)? (RW) -1.5 miles
6. What is the distance I traveled to where I stopped by the turkeys? (RW) $\mathbf{2 . 5}$ miles
7. Find the following for path $A$ in the diagram: (a) The
distance traveled. (b) The magnitude of the displacement from start to finish. (c) The displacement from start to finish. (OpenStax 2.1) $7 \mathrm{~m}, 7 \mathrm{~m}, 7 \mathrm{~m}$
8. Find the following for path $B$ in the diagram: (a) The
distance traveled. (b) The magnitude of the displacement
from start to finish. (c) The displacement from start to
distance traveled. (b) The magnitude of the displacement
from start to finish. (c) The displacement from start to finish. (OpenStax 2.2) $\mathbf{5 m} \mathbf{~ m} \mathbf{~ m}, \mathbf{- 5} \mathbf{~ m}$
9. Find the following for path C in the diagram: (a) The distance traveled. (b) The magnitude of the displacement from start to finish. (c) The displacement from start to finish. (OpenStax 2.3) $\mathbf{1 3} \mathbf{~ m , 9 \mathbf { m } , 9 \mathbf { m }}$
10. Find the following for path $D$ in the diagram: (a) The distance traveled. (b) The magnitude of the displacement from start to finish. (c) The displacement from start to finish. (OpenStax 2.4) $\mathbf{8 ~ m , 4 ~ m , - 4 ~ m ~}$
f. $\qquad$ In an experiment, a toy car moves -15 cm
g. $\qquad$ In an experiment, a mouse moves +20
cm
h. $\qquad$ The temperature is $-5^{\circ} \mathrm{C}$ (OpenStax 2,4$) 8 m, 4 m, 4 m$


## More about Velocity and Speed

- Velocity is the $\qquad$ of a distance vs time graph.

$$
\bar{v}=\frac{\Delta x}{\Delta t}=\frac{x-x_{0}}{t-t_{0}}
$$

- Often this is rewritten as

$$
x=\bar{v} t+x_{0}
$$

- If the graph is not a $\qquad$ line, then use the slope of a
$\qquad$ line drawn to that point.
- Velocity is a vector (has direction) $v=\frac{\text { displacement }}{\text { time }}$
- Speed is a scalar (no direction) $v=\frac{\text { distance }}{\text { time }}$
- Units of both are $\mathrm{m} / \mathrm{s}$


The graph shows the height of a ball thrown straight up vs time. Find the velocity of the ball at 2 seconds.

(a) Sketch a graph of velocity-time corresponding to the graph of displacement-time given in the graph. (b) Identify the time or times (etc.) at which the instantaneous velocity is greatest. (c) At which times is it zero? (d) At which times is it negative?


The spine-tailed swift is the fastest bird in powered flight. On one flight, a particular bird flies 306 m east, then turns around and flies 406.5 m back west. This flight takes 15 s . What is the bird's average velocity?

Average speed?

Which of these would we use to say how fast the bird is?

## Homework

1. What is the meaning of obtaining a negative velocity?
2. (a)Draw a quick sketch of position-time graph of a ball being thrown up so that it goes up, then comes back down. (b) Describe the graph using mathematical terms.
3. A bus makes a trip according to the position-time graph shown in the drawing. What is the average velocity (magnitude and direction) of the bus during each of the segments labeled A, B, and C? Express your answers in $\mathrm{km} / \mathrm{h}$. (Cutnell 2.48)
$-20 \mathrm{~km} / \mathrm{h}, 10 \mathrm{~km} / \mathrm{h}, 40 \mathrm{~km} / \mathrm{h}$

4. A person who walks for exercise produces the position-time graph given with this problem. (a) Without doing any calculations, decide which segments of the graph (A, B, C, or D) indicate positive, negative, and zero average velocities. (b) Calculate the average velocity for each segment to verify your answers to part (a).
(Cutnell 2.60) $6.3 \mathrm{~km} / \mathrm{h},-3.8 \mathrm{~km} / \mathrm{h}, 0.63 \mathrm{~km} / \mathrm{h}, 0 \mathrm{~km} / \mathrm{h}$
5. What is the difference between speed and velocity?
6. (a) Does a car's odometer measure distance or displacement? (b) Does its speedometer measure speed or velocity?
7. If you divide the total distance traveled on a car trip (as determined by the odometer) by the time for the trip, (a) are you calculating the average speed or the magnitude of the average velocity? (b) Under what circumstances are these two
 quantities the same?
8. Land west of the San Andreas fault in southern California is moving at an average velocity of about $6 \mathrm{~cm} / \mathrm{y}$ northwest relative to land east of the fault. Los Angeles is west of the fault and may thus someday be at the same latitude as San Francisco, which is east of the fault. How far in the future will this occur if the displacement to be made is 590 km northwest, assuming the motion remains constant? (OpenStax 2.8) $\mathbf{1} \times \mathbf{1 0}^{\mathbf{7}} \mathbf{~ y r s}$
9. Conversations with astronauts on the lunar surface were characterized by a kind of echo in which the earthbound person's voice was so loud in the astronaut's space helmet that it was picked up by the astronaut's microphone and transmitted back to Earth. It is reasonable to assume that the echo time equals the time necessary for the radio wave to travel from the Earth to the Moon and back (that is, neglecting any time delays in the electronic equipment). Calculate the distance from Earth to the Moon given that the echo time was 2.56 s and that radio waves travel at the speed of light $\left(3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}\right)$. (OpenStax 2.13) 384,000 km
10. A football quarterback runs 15.0 m straight forward 2.50 s . He is then hit and pushed 3.00 m straight backward in 1.75 s . He breaks the tackle and runs straight forward another 21.0 m in 5.20 s . Calculate his average velocity (a) for each of the three intervals and (b) for the entire motion. (OpenStax 2.14) $\mathbf{6 . 0 0} \mathbf{~ m} / \mathbf{s}, \mathbf{- 1 . 7 1} \mathbf{~ m} / \mathbf{s}, \mathbf{4 . 0 4} \mathbf{~ m} / \mathbf{s}, \mathbf{3 . 4 9 ~ m / s}$
11. As the Earth rotates through one revolution, a person standing on the equator traces out a circular path whose radius is equal to the radius of the earth $\left(6.38 \times 10^{6} \mathrm{~m}\right)$. What is the average speed of this person in meters per second? Miles per hour? (Cutnell 2.5) $\mathbf{4 6 4} \mathbf{~ m} / \mathrm{s}, 1040 \mathbf{m p h}$

## More about Acceleration

- Acceleration is how quickly $\qquad$ is changing.

$$
\begin{gathered}
a=\frac{\Delta v}{\Delta t}=\frac{v-v_{0}}{t-t_{0}} \\
v=a t+v_{0}
\end{gathered}
$$

- Acceleration is the $\qquad$ of a $\qquad$ vs time graph.
- Acceleration is a $\qquad$ (has direction).
- If the velocity and acceleration are the same direction, then the object $\qquad$ speed.
- If the velocity and acceleration are in opposite directions, then the object $\qquad$ speed.
- If there is constant acceleration
- The graph of position-time is $\qquad$ ( $x=\frac{1}{2} a t^{2}+v_{0} t+x_{0}$ is quadratic)
- The graph of velocity-time is $\qquad$ ( $v=a t+v_{0}$ is linear)

A dropped object near the earth will accelerate downward at $9.8 \mathrm{~m} / \mathrm{s}^{2}$. (Use $-9.8 \mathrm{~m} / \mathrm{s}^{2}$.) If the initial velocity is $1 \mathrm{~m} / \mathrm{s}$ downward, what will be its velocity at the end of 3 s ? Is it speeding up or slowing down?

## Homework

1. (a)Draw a quick sketch of velocity-time graph of a ball being thrown up so that it goes up, then comes back down. (b) Describe the graph using mathematical terms.
2. One way to find the acceleration due to gravity is to graph the position-time of a dropped object. How could you use the position-time graph to find constant acceleration?
3. A snowmobile moves according to the velocity-time graph shown in the drawing. What is the snowmobile's average acceleration during each of the segments A, B, and C? (Cutnell 2.59) $\mathbf{2 ~ m / s} \mathbf{s}^{\mathbf{2}}, \mathbf{0} \mathbf{~ m} / \mathbf{s}^{\mathbf{2}}, \mathbf{3 . 8} \mathbf{~ m} / \mathbf{s}^{\mathbf{2}}$

4. (a) By taking the slope of the curve in the position-time graph, verify that the velocity of the jet car is $115 \mathrm{~m} / \mathrm{s}$ at $\mathrm{t}=20 \mathrm{~s}$.
(b) By taking the slope of the curve at any point in the velocity-time graph, verify that the jet car's acceleration is $5.0 \mathrm{~m} / \mathrm{s}^{2}$. (OpenStax 2.59)

5. By taking the slope of the curve in graph, verify that the acceleration is $3.2 \mathrm{~m} / \mathrm{s}^{2}$ at $\mathrm{t}=10 \mathrm{~s}$. (OpenStax 2.62)

6. A graph of $v(t)$ is shown for a world-class track sprinter in a $100-\mathrm{m}$ race. (a) What is his average velocity for the first 4 s ? (b) What is his instantaneous velocity at $\mathrm{t}=5 \mathrm{~s}$ ? (c) What is his average acceleration between 0 and 4 s ? (d) What is his time for the race? (OpenStax 2.65 ) $\mathbf{6 m / s}, \mathbf{1 2 ~ m} / \mathrm{s}, \mathbf{3} \mathbf{~ m} / \mathrm{s}^{2}, \mathbf{1 0 ~ s}$
7. If a car is accelerating in the positive direction and is currently moving in the negative direction, (a) is it speeding up or slowing down? (b) How about if the acceleration is positive and the velocity is positive?
8. A cheetah can accelerate from rest to a speed of $30.0 \mathrm{~m} / \mathrm{s}$ in 7.00 s . What is its acceleration? (OpenStax 2.16) $4.29 \mathrm{~m} / \mathrm{s}^{2}$
9. Dr. John Paul Stapp was U.S. Air Force officer who studied the effects of extreme deceleration on the human body. On December 10, 1954, Stapp rode a rocket sled, accelerating from rest to a top speed of $282 \mathrm{~m} / \mathrm{s}(1015 \mathrm{~km} / \mathrm{h})$ in 5.00 s , and was brought jarringly back to rest in only 1.40 s! Calculate his (a) acceleration and (b) deceleration. Express each in multiples of $g\left(9.80 \mathrm{~m} / \mathrm{s}^{2}\right)$ by taking its ratio to the acceleration of gravity. (OpenStax 2.17 ) $56.4 \mathbf{~ m} / \mathbf{s}^{2}, 5.76 \mathrm{~g},-\mathbf{2 0 1} \mathrm{m} / \mathbf{s}^{2}$, 20.6 g
10. A motorcycle has a constant acceleration of $2.5 \mathrm{~m} / \mathrm{s}^{2}$. Both the velocity and acceleration of the motorcycle point in the same direction. How much time is required for the motorcycle to change its speed from (a) 21 to $31 \mathrm{~m} / \mathrm{s}$, and (b) 51 to 61 $\mathrm{m} / \mathrm{s}$ ? (Cutnell 2.13) $4.0 \mathrm{~s}, 4.0 \mathrm{~s}$
11. A runner accelerates to a velocity of $5.36 \mathrm{~m} / \mathrm{s}$ due west in 3.00 s . His average acceleration is $0.640 \mathrm{~m} / \mathrm{s}^{2}$, also directed due west. What was his velocity when he began accelerating? (Cutnell 2.15) $3.44 \mathrm{~m} / \mathbf{s} \mathbf{~ W}$
$\qquad$

## Equations of 1-D Motion

Assume $\qquad$ so $\qquad$ and acceleration is $\qquad$

$$
\begin{gathered}
x=\bar{v} t+x_{0} \\
\bar{v}=\frac{v_{0}+v}{2} \\
v=a t+v_{0} \\
x=\frac{1}{2} a t^{2}+v_{0} t+x_{0} \\
v^{2}=v_{0}^{2}+2 a\left(x-x_{0}\right)
\end{gathered}
$$

## Problem Solving Strategy

1. Examine the situation to determine which $\qquad$ are involved.
a. Maybe $\qquad$
2. Make a $\qquad$ of what is $\qquad$ or can be $\qquad$ from the problem.
3. Identify exactly what needs to be $\qquad$ in the problem.
4. Find an $\qquad$ or set of equations that can help you solve the problem.
5. $\qquad$ the knowns along with their $\qquad$ into the appropriate equation, and Solve
6. Check the answer to see if it is $\qquad$ : Does it make sense?

A plane starting from rest accelerates to $40 \mathrm{~m} / \mathrm{s}$ in 10 s . How far did the plane travel during this time?

To avoid an accident, a car decelerates at $0.50 \mathrm{~m} / \mathrm{s}^{2}$ for 3.0 s and covers 15 m of road. What was the car's initial velocity?

A cheetah is walking at $1.0 \mathrm{~m} / \mathrm{s}$ when it sees a zebra 25 m away. What acceleration would be required to reach $20.0 \mathrm{~m} / \mathrm{s}$ in that distance?

The left ventricle of the heart accelerates blood from rest to a velocity of $+26 \mathrm{~cm} / \mathrm{s}$. (a) If the displacement of the blood during the acceleration is +2.0 cm , determine its acceleration (in $\mathrm{cm} / \mathrm{s}^{2}$ ). (b) How much time does blood take to reach its final velocity?

## Homework

1. Is it possible for speed to be constant while acceleration is not zero? Give an example of such a situation.
2. Is it possible for velocity to be constant while acceleration is not zero? Explain.
3. Give an example in which velocity is zero yet acceleration is not.
4. An object moving with a constant acceleration can certainly slow down. But can an object ever come to a permanent halt if its acceleration truly remains constant? Explain.
5. A marble is dropped from 2.5 m and hits the ground in 0.71 s . What is the final velocity before it hits the ground? (RW) $7 \mathrm{~m} / \mathrm{s}$
6. A jet takes off from an aircraft carrier starting from rest and travels 93 m in 1.2 s when being pushed by the catapult. What is its final velocity at takeoff? (RW) $\mathbf{1 6 0} \mathbf{~ m} / \mathrm{s}$
7. An Olympic-class sprinter starts a race with an acceleration of $4.50 \mathrm{~m} / \mathrm{s}^{2}$. (a) What is her speed 2.40 s later? (b) Write an equation for position as a function of time. (c) Sketch a graph of her position vs. time for this period. (OpenStax 2.20) $\mathbf{1 0 . 8} \mathbf{~ m / s}$
8. Freight trains can produce only relatively small accelerations and decelerations. (a) What is the final velocity of a freight train that accelerates at a rate of $0.0500 \mathrm{~m} / \mathrm{s}^{2}$ for 8.00 min , starting with an initial velocity of $4.00 \mathrm{~m} / \mathrm{s}$ ? (b) If the train can slow down at a rate of $0.550 \mathrm{~m} / \mathrm{s}^{2}$, how long will it take to come to a stop from this velocity? (c) How far will it travel in each case? (OpenStax 2.29) $\mathbf{2 8 . 0} \mathbf{~ m} / \mathbf{s}, \mathbf{5 0 . 9} \mathbf{~ s}, 7680 \mathrm{~m}, 713 \mathrm{~m}$
9. A fireworks shell is accelerated from rest to a velocity of $65.0 \mathrm{~m} / \mathrm{s}$ over a distance of 0.250 m . (a) How long did the acceleration last? (b) Calculate the acceleration. (OpenStax 2.30) $\mathbf{7 . 6 9} \times \mathbf{1 0}^{-\mathbf{3}} \mathbf{s}, \mathbf{8 . 4 5} \times \mathbf{1 0}^{\mathbf{3}} \mathbf{~ m} / \mathbf{s}^{\mathbf{2}}$
10. A car skids to a stop to try to avoid hitting a deer. The car skids 21 m in 2.3 s . How fast was the car originally going? (RW) 18 m/s
11. What is the final velocity of a car that starts from rest and accelerates at $3.90 \mathrm{~m} / \mathrm{s}^{2}$ for a distance of 100 m ? (RW) 27.9 $\mathrm{m} / \mathrm{s}$
12. A hockey puck slides across the ice with an initial velocity of $7.2 \mathrm{~m} / \mathrm{s}$. It has a deceleration of $1.1 \mathrm{~m} / \mathrm{s}^{2}$ and is traveling toward the goal 5.0 m away. How much time does the goalie have to stop the puck? (RW) $\mathbf{0 . 7 4} \mathbf{~ s}$
13. If a moose can accelerate at $2.1 \mathrm{~m} / \mathrm{s}^{2}$ from rest, how much time will it take for it to accelerate to a speed of $4 \mathrm{~km} / \mathrm{h}$ ? (RW) 0.53 s
14. When you try to stop your car in an emergency, there is some time before you can react. Your car is going $25 \mathrm{~m} / \mathrm{s}$ and your reaction time is 0.20 s , then after you hit your brakes it decelerates at $9.5 \mathrm{~m} / \mathrm{s}^{2}$. How far will your car travel before it stops? (RW) $\mathbf{3 8} \mathbf{~ m}$

## Free Fall

Free fall is when an object is moving only under the influence of $\qquad$ _.

Ignoring air resistance, all objects fall to the earth with the $\qquad$ acceleration due to gravity (g)

$$
g=\square \frac{m}{s^{2}} .
$$

object thrown up, down, or dropped has this $\qquad$ -.
Use the one-dimensional $\qquad$
You drop a coin from the top of a hundred story building ( 1000 m ). If you ignore air resistance, how fast will it be falling right before it hits the ground?

How long does it take to hit the ground?

A baseball is hit straight up into the air. If the initial velocity was $20 \mathrm{~m} / \mathrm{s}$, how high will the ball go?

How long will it be until the catcher catches the ball at the same height it was hit?

## Homework

1. What is the acceleration of a rock thrown straight upward on the way up? At the top of its flight? On the way down?
2. An object that is thrown straight up falls back to Earth. This is one-dimensional motion. (a) When is its velocity zero? (b) Does its velocity change direction? (c) Does the acceleration due to gravity have the same sign on the way up as on the way down?
3. A penny is dropped from rest from the top of the Willis (Sears) Tower in Chicago. Considering that the height of the building is 427 m and ignoring air resistance, find the speed with which the penny strikes the ground. (Cutnell 2.37) 91.5 $\mathrm{m} / \mathrm{s}$
4. At the beginning of a basketball game, a referee tosses the ball straight up with a speed of $4.6 \mathrm{~m} / \mathrm{s}$. A player cannot touch the ball until after it reaches its maximum height and begins to fall down. What is the minimum time that a player must wait before touching the ball? (Cutnell 2.42) $\mathbf{0 . 4 7} \mathbf{~ s}$
5. A basketball referee tosses the ball straight up for the starting tipoff. At what velocity must a basketball player leave the ground to rise 1.25 m above the floor in an attempt to get the ball? (OpenStax 2.43) $4.95 \mathrm{~m} / \mathrm{s}$
6. A diver springs upward with an initial speed of $1.8 \mathrm{~m} / \mathrm{s}$ from a $3.0-\mathrm{m}$ board. (a) Find the velocity with which he strikes the water. (b) What is the highest point he reaches above the water? (Cutnell 2.44) -7.9 m/s, 3.2 m
7. (a) Calculate and graph the displacement at times of $0.500,1.00,1.50,2.00$, and 2.50 s for a rock thrown straight down with an initial velocity of $14.0 \mathrm{~m} / \mathrm{s}$ from the Verrazano Narrows Bridge in New York City. The roadway of this bridge is 70.0 m above the water. (b) Repeat, but now calculate and graph the velocity. (OpenStax 2.42)
$\mathbf{6 1 . 8} \mathrm{m}, \mathbf{5 1 . 1} \mathrm{m}, \mathbf{3 8 . 0} \mathrm{m}, 22.4 \mathrm{~m}, 4.4 \mathrm{~m} ;-18.9 \mathrm{~m} / \mathrm{s},-23.8 \mathrm{~m} / \mathrm{s},-28.7 \mathrm{~m} / \mathrm{s},-\mathbf{3 3 . 6} \mathrm{m} / \mathrm{s},-\mathbf{3 8 . 5} \mathrm{m} / \mathrm{s}$
8. A rescue helicopter is hovering over a person whose boat has sunk. One of the rescuers throws a life preserver straight down to the victim with an initial velocity of $1.40 \mathrm{~m} / \mathrm{s}$ and observes that it takes 1.8 s to reach the water. (a) List the knowns in this problem. (b) How high above the water was the preserver released? Note that the downdraft of the helicopter reduces the effects of air resistance on the falling life preserver, so that an acceleration equal to that of gravity is reasonable. (OpenStax 2.44 ) $\mathbf{1 8} \mathbf{~ m}$
9. A dolphin in an aquatic show jumps straight up out of the water at a velocity of $13.0 \mathrm{~m} / \mathrm{s}$. (a) List the knowns in this problem. (b) How high does his body rise above the water? To solve this part, first note that the final velocity is now a known and identify its value. Then identify the unknown, and discuss how you chose the appropriate equation to solve for it. After choosing the equation, show your steps in solving for the unknown, checking units, and discuss whether the answer is reasonable. (c) How long is the dolphin in the air? Neglect any effects due to his size or orientation. (OpenStax 2.45) $\mathbf{8 . 6 2 ~ m , ~} 2.65 \mathrm{~s}$
10. A very strong, but inept, shot putter puts the shot straight up vertically with an initial velocity of $11.0 \mathrm{~m} / \mathrm{s}$. How long does he have to get out of the way if the shot was released at a height of 2.20 m , and he is 1.80 m tall? (OpenStax 2.48 ) 2.28 s
11. You throw a ball straight up with an initial velocity of $15.0 \mathrm{~m} / \mathrm{s}$. It passes a tree branch on the way up at a height of 7.00 m . How much additional time will pass before the ball passes the tree branch on the way back down? (OpenStax 2.49) $1.91 \mathbf{s}$

## Vectors

- Vectors are measurements with $\qquad$ and $\qquad$ .
- They are represented by $\qquad$
- The length of the arrow is the $\qquad$ .
- The direction of the arrow is the $\qquad$ -.
- Can be represented in $\qquad$ form
- Make a $\qquad$ using the vector as the $\qquad$ _
- Use $\qquad$ and $\qquad$ to find the horizontal ( x ) component and the vertical (y) component
- Assign $\qquad$ signs to any component going $\qquad$ or $\qquad$
- $\sin (\theta)=\frac{\text { opposite }}{\text { hypotenuse }} \quad \cos (\theta)=\frac{\text { adjacent }}{\text { hypotenuse }} \quad \tan (\theta)=\frac{\text { opposite }}{\text { adjacent }}$

A football player kicks a ball at $15 \mathrm{~m} / \mathrm{s}$ at $30^{\circ}$ above the ground. Find the horizontal and vertical components
 of this velocity.

## Scalar Multiplication

- Multiplying a vector by a $\qquad$ number
- Draw the vector that many times in a $\qquad$
- Or multiply the $\qquad$ by that number
- A negative vector means multiply by -1 , so it goes in the $\qquad$ direction
Vector Addition - Graphical Method
- Draw the $\qquad$ vector.
- Draw the second vector where the $\qquad$ (tip-to-tail).
- Draw the resultant vector from where the $\qquad$ vector begins to where the
$\qquad$ vector ends.
$\bullet$ $\qquad$ the resultant's length and direction.


Add the following vectors graphically. $\boldsymbol{A}=2 \sqrt{2}$ at $45^{\circ} \mathrm{N}$ of $\mathrm{E}, \boldsymbol{B}=2 \sqrt{2}$ at $45^{\circ} \mathrm{W}$ of N .

## Vector Addition - Component Method

Vectors can be described by its
$\qquad$ to show how far it goes in the x and y directions. To add vectors, you simply add the $\qquad$ and components.
to get total
com

1. Find the
$\qquad$ the vectors to be added all the $\qquad$ components
2. $\qquad$ all the $\qquad$ components
3. $\qquad$ T

(a)

(b)

(c)
4. Use the $\qquad$ Theorem to find the $\qquad$ of the resultant
5. Use $\qquad$ to find the $\qquad$ (the direction is always found at the $\qquad$ of the resultant) Note: Drawing pictures and triangles helps immensely.

A jogger runs 145 m in a direction $20.0^{\circ}$ east of north and then 105 m in a direction $35.0^{\circ}$ south of east. Determine the magnitude and direction of jogger's position from her starting point.

## Homework

1. (a) Is it possible for one component of a vector to be zero, while the vector itself is not zero? (b) Is it possible for a vector to be zero, while one component is not zero? Explain.
2. Can two nonzero perpendicular vectors be added together so their sum is zero? Explain.
3. Can three or more vectors with unequal magnitudes be added together so their sum is zero? If so, show by means of a tip-to-tail arrangement of the vectors how this could occur.
4. Suppose you first walk 12.0 m in a direction $20^{\circ}$ west of north and then 20.0 m in a direction $40.0^{\circ}$ south of west. How far are you from your starting point, and what is the compass direction of a line connecting your starting point to your final position? Solve this graphically. (OpenStax 3.5 ) $\mathbf{1 9 . 5} \mathbf{m}$ at $4.65^{\circ} \mathrm{S}$ of $\mathbf{W}$
5. An ostrich is running at a speed of $17.0 \mathrm{~m} / \mathrm{s}$ in a direction of $68.0^{\circ}$ north of west. What is the magnitude of ostrich's velocity component that is directed (a) due north and (b) due west? (RW) $15.8 \mathrm{~m} / \mathrm{s}, 6.37 \mathrm{~m} / \mathrm{s}$
6. An ocean liner leaves New York City and travels $18.0^{\circ}$ north of east for 155 km . How far east and how far north has it gone? In other words, what are the magnitudes of the components of the ship's displacement vector in the directions (a) due east and (b) due north? (Cutnell 1.33 ) $\mathbf{1 4 7}$ km, $\mathbf{4 7 . 9} \mathbf{~ k m}$
7. A new landowner has a triangular piece of flat land she wishes to fence. Starting at the west corner, she measures the first side to be 80.0 m long and the next to be 105 m . These sides are represented as displacement vectors A and B in Figure 3.61. She then correctly calculates the length and orientation of the third side $C$. What is her result? (Hint: Since $A+B+C=0$, then $A+$ $B=-C$.) (OpenStax 3.20) $\mathbf{9 2 . 3} \mathbf{m}$ at $53 . \mathbf{7}^{\circ} \mathbf{S}$ of $\mathbf{W}$
8. A golfer, putting on a green, requires three strokes to "hole the ball." During the first putt, the ball rolls 5.0 m due east. For the second putt, the ball travels 2.1 m at an angle of $20.0^{\circ}$ north of east. The third putt is 0.50 m due north. What displacement (magnitude and direction relative to due east) would have been needed to "hole the ball" on the very first putt? (Cutnell 1.41) 7.1 $m$ at $9.9^{\circ} \mathrm{N}$ of E

9. You are on a treasure hunt and your map says, "Walk due west for 52 paces, then walk $30.0^{\circ}$ north of west for 42 paces, and finally walk due north for 25 paces." What is the magnitude of the component of your displacement (a) due north and (b) due west? (Cutnell 1.42) 46 paces, 88 paces
10. On a safari, a team of naturalists sets out toward a research station located 4.8 km away in a direction $42^{\circ}$ north of east. After traveling in a straight line for 2.4 km , they stop and discover that they have been traveling $22^{\circ}$ north of east, because their guide misread his compass. What are (a) the magnitude and (b) the direction (relative to due east) of the displacement vector now required to bring the team to the research station? (Cutnell 1.45) $2.7 \mathbf{~ k m}$ at $\mathbf{6 0}^{\circ} \mathbf{N}$ of $\mathbf{E}$
11. While snorkeling in the ocean, you swim directly towards shore at $2 \mathrm{~m} / \mathrm{s}$. The current of the water pushes you directly sideways at 3 $\mathrm{m} / \mathrm{s}$. What is your resultant velocity (magnitude and direction relative to your intended path of straight towards shore)? (RW) $3.6 \mathbf{~ m} / \mathbf{s}$ at $56.3^{\circ}$
12. An airplane flies at $200 \mathrm{~km} / \mathrm{h}$ at $30.0^{\circ} \mathrm{N}$ of W . The wind blows it at $30 \mathrm{~km} / \mathrm{h}$ at $45.0^{\circ} \mathrm{E}$ of N . What is the resultant velocity of the airplane (magnitude and direction)? (RW) $194 \mathbf{~ k m} / \mathrm{h}$ at $38.6^{\circ} \mathrm{N}$ of $\mathbf{W}$
13. You are trying to row a boat directly across a river that is 50.0 m wide. You can row at $3.1 \mathrm{~m} / \mathrm{s}$ in a direction directly across the river perpendicular to the shore. The current is $4.8 \mathrm{~m} / \mathrm{s}$ parallel to shore. (a) What is your velocity relative to the shore? (b) How much time does it take to get to the other side of the river? (c) How far down stream do you land? (RW) $5.71 \mathrm{~m} / \mathbf{s}$ at $32.9^{\circ}$ downstream from shore, $16.1 \mathrm{~s}, 77.7 \mathrm{~m}$

## Name:

- Objects in $\qquad$ only under influence of $\qquad$
- $\quad x$ and $y$ components are $\qquad$ -
- ____ is only quantity that is the $\qquad$ in both dimensions
- x-component velocity $\qquad$ since nothing pulling it sideways
- Use $\qquad$
- y-component $\qquad$ because gravity pulling it down
- Use $\qquad$
- If the starting and ending height are the $\qquad$ the distance the object goes can be found with the $\qquad$ equation.


A Veggie-meatball with $v=5.0 \mathrm{~m} / \mathrm{s}$ rolls off a 1.0 m high table. How long does it take to hit the floor if no one sneezes?

What is its velocity when it hits the floor?

A truck ( $\mathrm{v}=11.2 \mathrm{~m} / \mathrm{s}$ ) turned a corner too sharp and lost part of the load. A falling box will break if it hits the ground with a velocity greater than $15 \mathrm{~m} / \mathrm{s}$. The height of the truck bed is 1.5 m . Will the box break?

While driving down a road a bad guy shoots a bullet straight up into the air. If there was no air resistance where would the bullet land in front, behind, or on him?

If a gun were fired horizontally and a bullet were dropped from the same height at the same time, which would hit the ground first?

A batter hits the ball at $35^{\circ}$ with a velocity of $32 \mathrm{~m} / \mathrm{s}$. How high did the ball go?

How long was the ball in the air?

How far did the ball go?

## Homework

1. Is the acceleration of a projectile equal to zero when it reaches the top of its trajectory? If not, why not?
2. A tennis ball is hit upward into the air and moves along an arc. Neglecting air resistance, where along the arc is the speed of the ball (a) a minimum and (b) a maximum? Justify your answers.
3. A tennis ball is hit upward into the air and moves along an arc. Neglecting air resistance, where along the arc is the acceleration of the ball (a) a minimum and (b) a maximum? Justify your answers.
4. A wrench is accidentally dropped from the top of the mast on a sailboat. Will the wrench hit at the same place on the deck whether the sailboat is at rest or moving with a constant velocity? Justify your answer.
5. A stone is thrown horizontally from the top of a cliff and eventually hits the ground below. A second stone is dropped from rest from the same cliff, falls through the same height, and also hits the ground below. Ignore air resistance. Discuss whether each of the following quantities is different or the same in the two cases; if there is a difference, describe the difference: (a) displacement, (b) speed just before impact with the ground, and (c) time of flight.
6. A projectile is launched at ground level with an initial speed of $50.0 \mathrm{~m} / \mathrm{s}$ at an angle of $30.0^{\circ}$ above the horizontal. It strikes a target above the ground 3.00 seconds later. What are the $x$ and $y$ distances where the projectile was launched to where it lands? (OpenStax 3.25) $\mathbf{1 . 3 0} \times \mathbf{1 0}^{\mathbf{2}} \mathbf{m , 3 0 . 9} \mathbf{~ m}$
7. A ball is thrown horizontally from the top of a $60.0-\mathrm{m}$ building and lands 100.0 m from the base of the building. Ignore air resistance. (a) How long is the ball in the air? (b) What must have been the initial horizontal component of the velocity? (c) What is the vertical component of the velocity just before the ball hits the ground? (d) What is the velocity (including both the horizontal and vertical components) of the ball just before it hits the ground? (OpenStax 3.27) $\mathbf{3 . 5 0} \mathbf{s}, \mathbf{2 8 . 6} \mathbf{~ m} / \mathbf{s}, \mathbf{- 3 4 . 3}$ $\mathrm{m} / \mathrm{s}, 44.7 \mathrm{~m} / \mathrm{s}$ at $50.2^{\circ}$ below x -axis
8. (a) A daredevil is attempting to jump his motorcycle over a line of buses parked end to end by driving up a 32 웅 rat a speed of $40.0 \mathrm{~m} / \mathrm{s}(144 \mathrm{~km} / \mathrm{h})$. How many buses can he clear if the top of the takeoff ramp is at the same height as the bus tops and the buses are 20.0 m long? (b) Discuss what your answer implies about the margin of error in this act-that is, consider how much greater the range is than the horizontal distance he must travel to miss the end of the last bus.
(Neglect air resistance.) (OpenStax 3.28) 7 buses
9. An arrow is shot from a height of 1.5 m toward a cliff of height H . It is shot with a velocity of $30 \mathrm{~m} / \mathrm{s}$ at an angle of $60^{\circ}$ above the horizontal. It lands on the top edge of the cliff 4.0 s later. (a) What is the height of the cliff? (b) What is the maximum height reached by the arrow along its trajectory? (c) What is the arrow's impact speed just before hitting the cliff? (OpenStax 3.34 ) $\mathbf{2 7 . 0} \mathbf{m}, \mathbf{3 6 . 0} \mathbf{~ m , ~} \mathbf{2 0} \mathbf{~ m} / \mathrm{s}$
10. The world long jump record is 8.95 m (Mike Powell, USA, 1991). Treated as a projectile, what is the maximum range obtainable by a person if he has a take-off speed of $9.5 \mathrm{~m} / \mathrm{s}$ ? State your assumptions. (OpenStax 3.36) $9.21 \mathbf{~ m}$
11. An eagle is flying horizontally at a speed of $3.00 \mathrm{~m} / \mathrm{s}$ when the fish in her talons wiggles loose and falls into the lake 5.00 m below. Calculate the velocity of the fish relative to the water when it hits the water. (OpenStax 3.40 ) $\mathbf{1 0 . 3} \mathbf{~ m} / \mathbf{s}, \mathbf{7 3 . 1}{ }^{\circ}$ below the horizontal
12. Can a goalkeeper at his goal kick a soccer ball into the opponent's goal without the ball touching the ground? The distance will be about 95 m . A goalkeeper can give the ball a speed of $30 \mathrm{~m} / \mathrm{s}$. (OpenStax 3.43) $\mathbf{9 1 . 8} \mathbf{~ m}$, No
13. A tennis ball is struck such that it leaves the racket horizontally with a speed of $28.0 \mathrm{~m} / \mathrm{s}$. The ball hits the court at a horizontal distance of 19.6 m from the racket. What is the height of the tennis ball when it leaves the racket? (OpenStax 3.14) 2.40 m
14. A diver runs horizontally with a speed of $1.20 \mathrm{~m} / \mathrm{s}$ off a platform that is 10.0 m above the water. What is his speed just before striking the water? (RW) $\mathbf{1 4 . 1} \mathbf{~ m / s}$
15. The 1994 Winter Olympics included the aerials competition in skiing. In this event skiers speed down a ramp that slopes sharply upward at the end. The sharp upward slope launches them into the air, where they perform acrobatic maneuvers. In the women's competition, the end of a typical launch ramp is directed $63^{\circ}$ above the horizontal. With this launch angle, a skier attains a height of 13 m above the end of the ramp. What is the skier's launch speed? (Cutnell 3.24 ) $\mathbf{1 8} \mathbf{~ m} / \mathbf{s}$

## Physics

Unit 1: Introduction and Kinematics Review

1. Know about scientific method, units, fundamental units, unit prefixes, precision, accuracy, significant figures, vectors, scalars
2. Convert 120 Tm to m
3. In the process of delivering milk, a milkman, walks 100 m due east from his truck. He then turns around and walks 20 m due west. What is the milkman's displacement relative to his truck (magnitude and direction)? What distance did he travel?
4. A pigeon flew 10 km across town with an average speed of $5 \mathrm{~m} / \mathrm{s}$. How long, in hours, did it take the pigeon to make this journey?
5. A car, starting from rest, accelerates in a straight-line path at a constant rate of $2 \mathrm{~m} / \mathrm{s}^{2}$. How far will the car travel in 10 seconds?
6. The minimum takeoff speed for a certain airplane is $50 \mathrm{~m} / \mathrm{s}$. What minimum acceleration is required if the plane must leave a runway of length 2000 m ? Assume the plane starts from rest at one end of the runway.
7. Water drips from rest from a leaf that is $2 m$ above the ground. Neglecting air resistance, what is the speed of each water drop when it hits the ground?
8. What maximum height will be reached by a stone thrown straight up with an initial speed of $5 \mathrm{~m} / \mathrm{s}$ ?
9. A cheetah is walking at a speed of $0.5 \mathrm{~m} / \mathrm{s}$ when it observes a gazelle 15 m directly ahead. If the cheetah accelerates at 3 $\mathrm{m} / \mathrm{s}^{2}$, how long does it take the cheetah to reach the gazelle if the gazelle doesn't move?
10. Be able to read graphs and calculate speed, velocity, and acceleration from them.
11. A jumper in the long-jump goes into the jump with a speed of $5 \mathrm{~m} / \mathrm{s}$ at an angle of $20^{\circ}$ above the horizontal. What is the jumper's horizontal speed as they jump? What is their vertical speed?
12. A sailboat leaves a harbor and sails 21 km in the direction $15^{\circ}$ north of east, where the captain stops for lunch. A short time later, the boat sails 2 km in the direction $75^{\circ}$ south of east. What is the magnitude of the resultant displacement?
13. An eagle is flying due east at $5 \mathrm{~m} / \mathrm{s}$ carrying a gopher in its talons. The gopher manages to break free at a height of 50 m . What is the magnitude of the gopher's velocity as it reaches the ground?
14. A ball is thrown horizontally from the top of a 100 m tall building with an initial speed of $5 \mathrm{~m} / \mathrm{s}$. How far from the base of the building did the ball land?
15. A swimmer swims with a velocity of $15 \mathrm{~m} / \mathrm{s}$ south relative to the water. The current of the water is $2 \mathrm{~m} / \mathrm{s}$ relative to the shore. If the current is moving west, what is the velocity of the swimmer relative to the shore?
16. Displacement: $100 m-20 m=\mathbf{8 0} \boldsymbol{m}$;

Distance: $100 m+20 m=120 m$
4. $\bar{v}=5 \frac{\mathrm{~m}}{\mathrm{~s}}, \Delta x=10 \mathrm{~km}$

Convert: $\frac{10 \mathrm{~km}}{\left(\frac{10^{3} \mathrm{~m}}{1 \mathrm{~km}}\right)=10000 \mathrm{~m}, ~}$
$\bar{v}=\frac{\Delta x}{\Delta t}$
$5 \frac{\mathrm{~m}}{\mathrm{~s}}=\frac{10000 \mathrm{~m}}{t}$
$t=\frac{10000 \mathrm{~m}}{5 \frac{\mathrm{~m}}{\mathrm{~s}}}=2000 \mathrm{~s}$
Convert: $\frac{2000 s}{}\left(\frac{1 h}{3600 s}\right)=0.56 h$
5. $\quad a=2 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}, t=10 \mathrm{~s}, v_{0}=0 \frac{\mathrm{~m}}{\mathrm{~s}}, x=$ ?
$x=x_{0}+v_{0} t+\frac{1}{2} a t^{2}$
$x=0 m+\left(0 \frac{m}{s}\right)(10 s)+\frac{1}{2}\left(2 \frac{m}{s^{2}}\right)(10 s)^{2}$
$x=100 \mathrm{~m}$
6. $v=50 \frac{\mathrm{~m}}{\mathrm{~s}}, x=2000 \mathrm{~m}, v_{0}=0 \frac{\mathrm{~m}}{\mathrm{~s}}, a=$ ?
$v^{2}=v_{0}^{2}+2 a\left(x-x_{0}\right)$
$\left(50 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}=\left(0 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}+2 a(2000 m-0 m)$
$2500 \frac{\mathrm{~m}^{2}}{\mathrm{~s}^{2}}=(4000 \mathrm{~m}) a$
$a=0.625 \mathrm{~m} / \mathrm{s}^{2}$
7. $y_{0}=2 m, v_{0}=0 \frac{\mathrm{~m}}{\mathrm{~s}}, a=-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}, v=$ ?
$v^{2}=v_{0}^{2}+2 a\left(y-y_{0}\right)$
$v^{2}=\left(0 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}+2\left(-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right)(0 \mathrm{~m}-2 \mathrm{~m})$
$v^{2}=39.2 \frac{\mathrm{~m}^{2}}{\mathrm{~s}^{2}}$
$v=6.26 \frac{\mathrm{~m}}{\mathrm{~s}}$
8. $v_{0}=5 \frac{\mathrm{~m}}{\mathrm{~s}}, v=0 \frac{\mathrm{~m}}{\mathrm{~s}}, a=-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}, y=$ ?
$v^{2}=v_{0}^{2}+2 a\left(y-y_{0}\right)$
$\left(0 \frac{m}{s}\right)^{2}=\left(5 \frac{m}{s}\right)^{2}+2\left(-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right)(y-0 \mathrm{~m})$
$-25 \frac{\mathrm{~m}^{2}}{\mathrm{~s}^{2}}=\left(-19.6 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right) y$
$y=1.28 \mathrm{~m}$
9. $v_{0}=0.5 \frac{\mathrm{~m}}{\mathrm{~s}}, x=15 \mathrm{~m}, a=3 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}, t=$ ?
$x=x_{0}+v_{0} t+\frac{1}{2} a t^{2}$
$15 m=0 m+\left(0.5 \frac{\mathrm{~m}}{\mathrm{~s}}\right) t+\frac{1}{2}\left(3 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right) t^{2}$
$0=\left(\frac{3}{2} \frac{m}{s^{2}}\right) t^{2}+\left(0.5 \frac{\mathrm{~m}}{\mathrm{~s}}\right) t-15 \mathrm{~m}$
$t=\frac{-0.5 \pm \sqrt{(0.5)^{2}-4\left(\frac{3}{2}\right)(-15)}}{2\left(\frac{3}{2}\right)}=\mathbf{3 s},=3.33 \mathrm{~s}$
11. Horizontal: $v_{0 x}=5 \frac{\mathrm{~m}}{\mathrm{~s}} \cos 20^{\circ}=\mathbf{4 . 7 0} \frac{\mathrm{m}}{\mathrm{s}}$

Vertical: $v_{0 y}=5 \frac{\mathrm{~m}}{\mathrm{~s}} \sin 20^{\circ}=\mathbf{1} .71 \frac{\mathrm{~m}}{\mathrm{~s}}$
12.

|  | $x$ | $y$ |
| :--- | :--- | :--- |
| $21 \mathrm{~km} @ 15^{\circ} \mathrm{N}$ of $E$ | 20.28 | 5.44 |
| 2 km @ $75^{\circ} \mathrm{S}$ of E | 0.52 | -1.93 |
|  | 20.80 | 3.51 |

$r=\sqrt{20.80^{2}+3.51^{2}}=21.1 \mathrm{~km}$
$\theta=\tan ^{-1} \frac{3.51}{20.80}=9.67^{\circ} \mathrm{N}$ of $E$
13. $x: v_{0 x}=5 \frac{\mathrm{~m}}{\mathrm{~s}}, y: v_{0 y}=0 \frac{\mathrm{~m}}{\mathrm{~s}}, y_{0}=50 \mathrm{~m}, a_{y}=$
$-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}, y=0 \mathrm{~m}, v_{y}=$ ?
$v_{y}^{2}=v_{0 y}^{2}+2 a_{y}\left(y-y_{0}\right)$
$v_{y}^{2}=\left(0 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}+2\left(-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right)(0 \mathrm{~m}-50 \mathrm{~m})$
$v_{y}^{2}=980 \frac{\mathrm{~m}}{\mathrm{~s}}$
$v_{y}=31.30 \frac{\mathrm{~m}}{\mathrm{~s}}$
combine: $v=\sqrt{v_{x}^{2}+v_{y}^{2}}$
$v=\sqrt{\left(5 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}+\left(31.30 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}}=\mathbf{3 1 . 7 \mathrm { m } / \mathrm { s }}$
14. $x: v_{0 x}=5 \frac{\mathrm{~m}}{\mathrm{~s}}, x=? ; y: y_{0}=100 \mathrm{~m}, y=0 \mathrm{~m}, a=$
$-9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}, v_{0 y}=0 \frac{\mathrm{~m}}{\mathrm{~s}}$
find $t: y=y_{0}+v_{0 y} t+\frac{1}{2} a t^{2}$
$0 m=100 m+\left(0 \frac{m}{s}\right) t+\frac{1}{2}\left(-9.8 \frac{m}{s^{2}}\right) t^{2}$
$-100 m=\left(-4.9 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right) t^{2}$
$20.41 \frac{\mathrm{~m}^{2}}{\mathrm{~s}^{2}}=t^{2}$
$t=4.52 \mathrm{~s}$
find $x: x=x_{0}+v_{0 x} t$
$x=0+\left(5 \frac{\mathrm{~m}}{\mathrm{~s}}\right)(4.52 \mathrm{~s})=\mathbf{2 2 . 6} \mathbf{m}$
15. $v_{S W}=15 \frac{\mathrm{~m}}{\mathrm{~s}}$ South, $v_{W G}=2 \frac{\mathrm{~m}}{\mathrm{~s}}$ West
$v_{S G}=v_{S W}+v_{W G}$

|  | $x$ | $y$ |
| :--- | :--- | :--- |
| $15 \mathrm{~m} / \mathrm{s} \mathrm{S}$ | 0 | -15 |
| $2 \mathrm{~m} / \mathrm{s} \mathrm{W}$ | -2 | 0 |
|  | -2 | -15 |

$v_{S G}=\sqrt{(-2)^{2}+(-15)^{2}}=15.1 \mathrm{~m} / \mathrm{s}$
$\theta=\tan ^{-1}-\frac{15}{-2}=82.4^{\circ}$
$v_{S G}=15.1 \frac{\mathrm{~m}}{\mathrm{~s}}$ at $82.4^{\circ} S$ of $W$

